Directions: Write your name and school name on every sheet, and write your answers on the answer sheet. **DO NOT detach the answer sheet from your exam.** Answers can be given as integers, fractions or in decimal form. Answers given in decimal form should include no more than 4 places after the decimal, and the answer should be <u>accurate to 4</u> <u>places after the decimal</u>.

DO NOT ROUND YOUR ANSWERS!!

Example 1: You work on a problem, and your calculator gives the value 0.9092974268. **Correct Answer:** 0.9092 **Incorrect Answer:** 0.9093 **DO NOT ROUND.**

Example 2: You determine that the answer to a question is 1/2. **Correct Answer:** 1/2 **Correct Answer:** 0.5

Example 3: You determine that the answer to a question is 10/11, and your calculator tells you this has a decimal expansion 0.90909090... Correct Answer: 10/11 Correct Answer: 0.9090 Incorrect Answer: 0.9091 DO NOT ROUND.

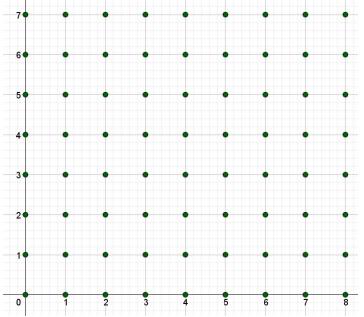
Good Luck!!

- 1. Give the number of seconds in a week.
- 2. Give the area of a circle with diameter 3.
- 3. Simplify

$$\frac{\left(3^{-5.1} + 7.21\sqrt{3.21 + \frac{1}{12}}\right)^{2.13}}{21.92 - \frac{14.36}{3}}$$

- 4. Give the value of x where the function $f(x) = x^4 3x^3 + 2x 1$ has its smallest value.
- 5. Give the distance between the points (-1,3) and (17,13).
- 6. Give the sum of the two largest x coordinates for the points of intersection of the line y = -x and the graph of $f(x) = x^4 3x^3 + 2x 1$.
- 7. Find 20% of 30% of 40% of 50% of ... of 200% of 1,432.
- 8. $\binom{13x 17y = 61}{31x + 43y = 37}$. Give the value of x + y.
- 9. Give the slope of a line that is perpendicular to the line that passes through the points (141.23, -137.22) and (211.47, -643.36).
- 10. $g(x) = \frac{1}{2x+3}$. Give the average of the numbers in the set $\{g(1), g(2), g(3), \dots, g(100)\}$
- 11. $f(x) = 3x x^2$ and $x_0 = 1.1$. Also, $x_1 = f(x_0)$, $x_2 = f(x_1)$, $x_3 = f(x_2)$, ..., $x_{100} = f(x_{99})$. Give the value of x_{100} .

- 12. Give the sum of the reciprocals of the solutions to $x^4 - 205x^3 - 397x^2 + 1946 = 0$
- 13. Write the base 5 representation of the base 10 number 10,321.
- 14. If p > 3 is a prime number, then $F_p = \{0, 1, 2, ..., p 1\}$. It is known that 937 is a prime number. There is a unique number $x \in F_{937}$ so that $17x = 1 \mod 937$. Give the value of x.
- 15. The set F_p was defined in the previous problem. There are unique values $x, y \in F_{47}$ so that $\begin{pmatrix} 3x + 11y = 23 \mod 47 \\ -29x + 36y = 11 \mod 47 \end{pmatrix}$. Give the value of x.
- 16. Give the sum of the lengths of all of the line segments with slope 1 or -1 that connect 2 points in the diagram below.



- 17. Give the slope of the line of best fit (least squares method) for the data (-1, -2), (3,1), (5,3) and (6,4).
- 18. Give the sum of the numbers in the set {1,2,3, ...,859} that are not integer multiples of 2, 3 or 7.

- 19. Two circles of radius 3 are centered at (0,0) and (3,0) respectively. What is the area of the region that lies inside both circles?
- 20. A point (a, b) is an integer point if both a and b are integers. Give the number of integer points that lie strictly inside the ellipse $x^2 + \frac{101,761}{47.089}y^2 = 101,761$.
- 21. Give the largest integer n so that $1 \quad 1$

$$1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} < 9.5$$

- 22. A curve is parameterized by $x(t) = 3t^2 9$ and $y(t) = 3t t^3$ for $-2 \le t \le 2$. There are three values of *b* so that the line y = x + b intersects the graph of this parameterized curve in two points, with one of the points having *y*-coordinate 1. Give the value of *b* so that the distance between these 2 points is as large as possible.
- 23. m < 2, and the lines y = 2x 1, y = 3x + 2 and y = mx + 1 are used to form a triangle with area 8.3671. Give the value of m.
- 24. Four integers are chosen at random from the set {1,2,3,...,21}. The values do not have to be distinct. What is the probability that the sum of the chosen values is strictly less than 49?
- 25. Give the average of the answers to problems 1 through 24.